

# Progress report for $71 \leq Z \leq 79$ odd- $Z$ nuclei

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- Current progress for odd- $Z$  nuclei (from  ${}_{71}\text{Lu}$  to  ${}_{79}\text{Au}$ )
- Comparison of the odd- $Z$  nuclei with experimental data and RCHB
- Properties of odd- $Z$  nuclei

# Nuemrical conditions and progress of odd- $Z$ nuclei

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- Nuclei: Odd- $Z$   ${}_{71}\text{Lu}$ ,  ${}_{73}\text{Ta}$ ,  ${}_{75}\text{Re}$ ,  ${}_{77}\text{Ir}$ , and  ${}_{79}\text{Au}$  isotopes
  - Version: `Code_DRHBC_202112`
  - Box size:  $R_{\text{box}} = 20$  fm
  - Mesh size:  $\Delta r = 0.1$  fm
  - Energy cutoff:  $E_{\text{cut}} = 300$  MeV
  - Angular momentum cutoff:  $J_{\text{max}} = 23/2 \hbar$  (jmx=12 in paramet.for)
  - Legendre expansion order:  $\lambda_{\text{max}} = 8$  (mlb=5 in paramet.for)
  - Relativistic density functional: PC-PK1
  - Pairing strength:  $-325.0$  MeV  $\cdot$  fm<sup>3</sup>
  - Initial deformations:  $\beta = -0.4, -0.3, -0.2, -0.1, 0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6$ , and so on
  - Blocking procedure: `Automatic blocking procedure`
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- All the ground states of odd- $Z$  nuclei have been determined by checking the potential energy curves of each nucleus.

# Progress of odd- $Z$ nuclei

## Proton drip line ( $71 \leq Z \leq 80$ )

X. Xia *et al.*, ADNDT **121**, 1 (2024).

P. Guo *et al.*, ADNDT **158**, 101661 (2024).

	Lu	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg
DRHBc	83	81	86	83	88	87	92	91	98*	92
RCHB	84	81	86	83	88	85	90	88	91	90

Neutron drip line ( $71 \leq Z \leq 80$ ): 184

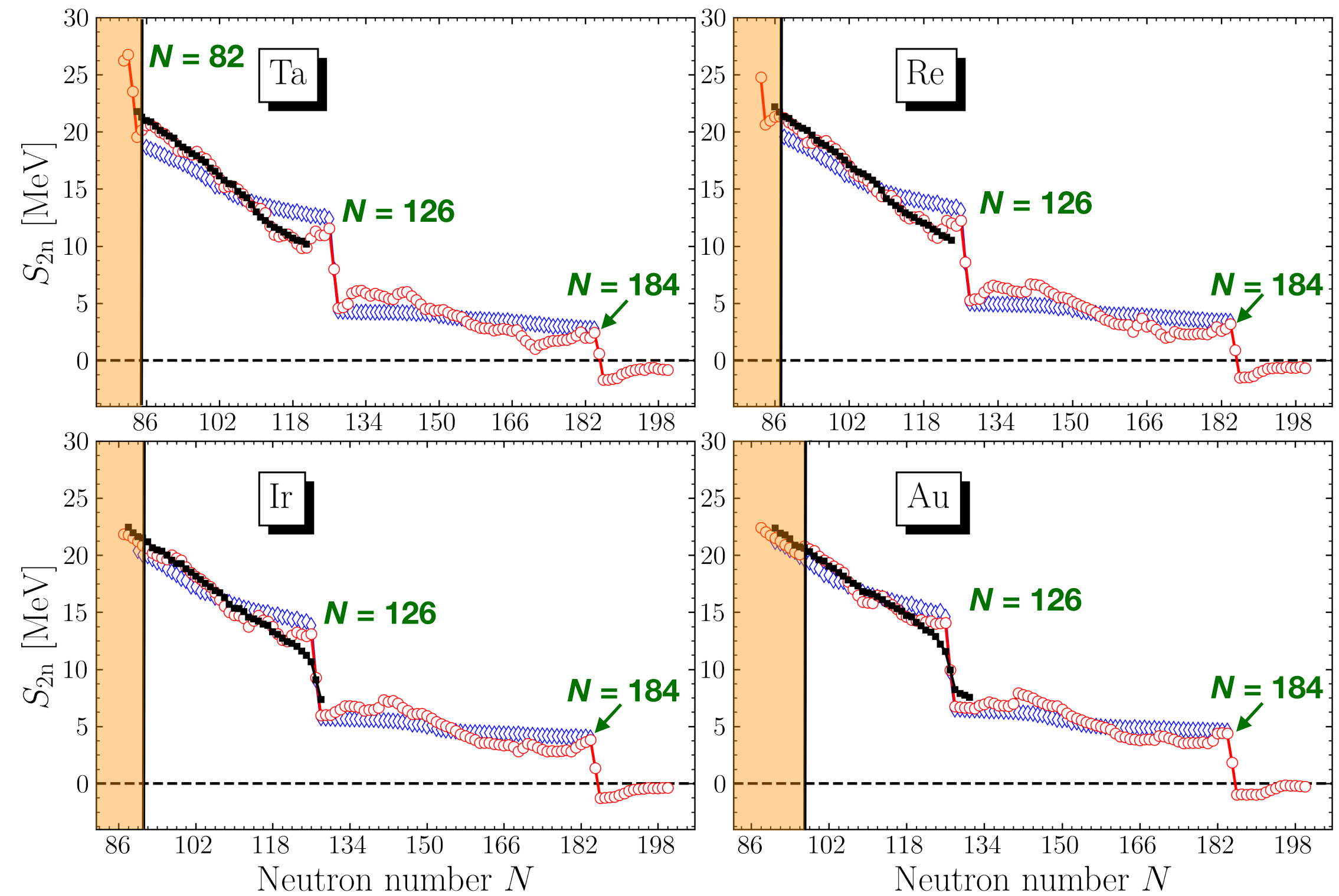
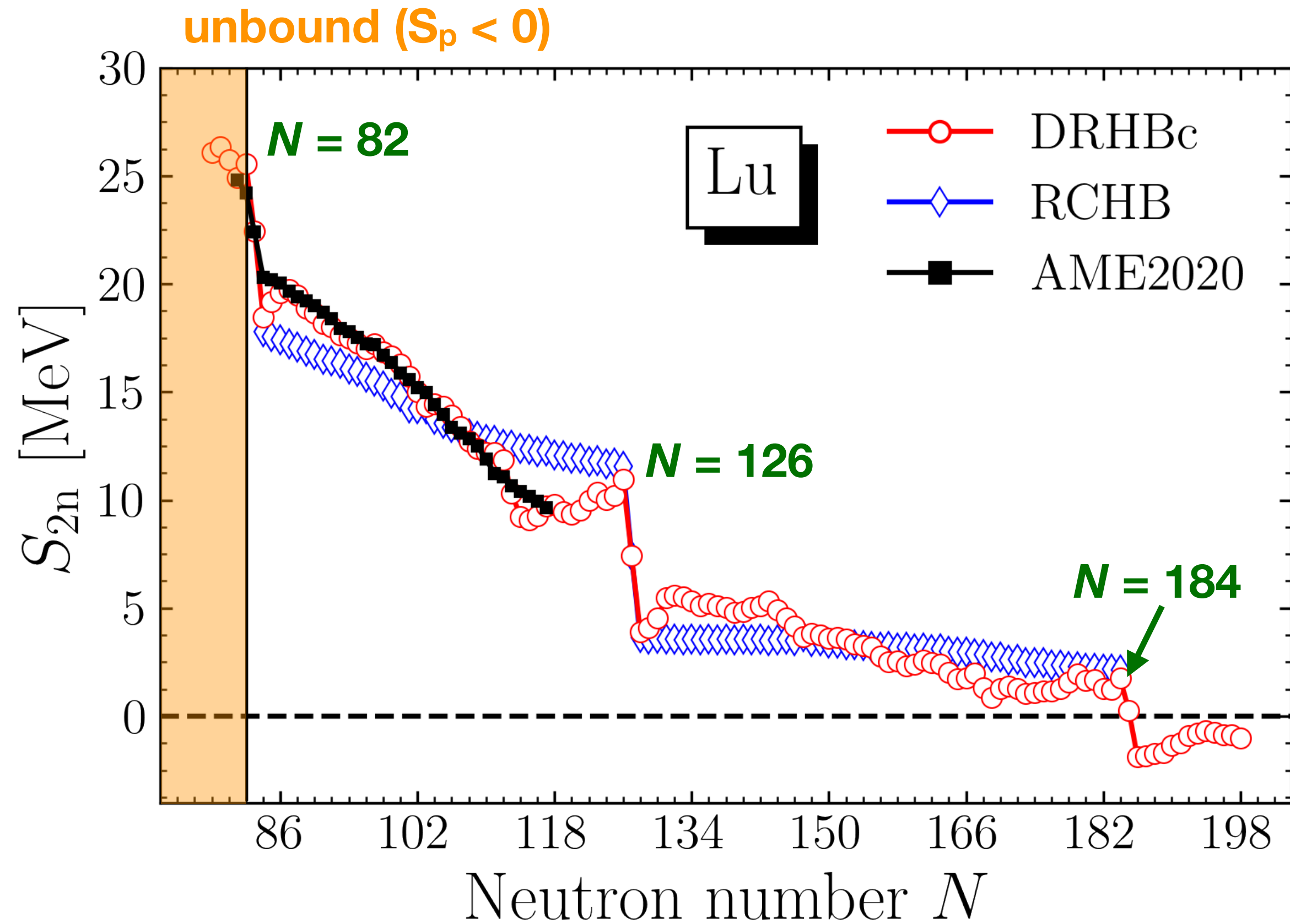
\*Constrained by binding energies of Pt isotopes

## Part of data table of Au isotopes

$A$	$N$	$E_b^{\text{Cal}}$ (MeV)	$E_{b+\text{rot}}^{\text{Cal}}$ (MeV)	$E_B^{\text{Exp}}$ (MeV)	$S_{2n}$ (MeV)	$S_{2p}$ (MeV)	$S_n$ (MeV)	$S_p$ (MeV)	$\lambda_n$ (MeV)	$\lambda_p$ (MeV)	$m^\pi(N)$	$m^\pi(P)$
165	86	1258.70	1258.70			-1.29		-1.67	-11.287	0.74		1/2+
166	87	1269.12	1270.26			-1.15	10.42	-1.50	-11.303	0.15	5/2-	1/2-
167	88	1281.09	1282.19		22.39	-0.67	11.97	-1.20	-11.112	-0.088		1/2-
168	89	1291.13	1292.37	1291.584	22.02	-0.62	10.05	-1.21	-11.026	0.50	1/2-	11/2-
169	90	1302.82	1304.33	1304.004	21.73	-0.15	11.69	-0.90	-10.850	0.20		11/2-
170	91	1312.64	1314.10	1314.100	21.51	0.02	9.82	-0.76	-10.634	0.02	1/2-	11/2-
171	92	1324.06	1325.67	1325.952	21.24	0.48	11.41	-0.52	-10.558	-0.202		11/2-
172	93	1333.54	1335.00	1335.779	20.90	0.73	9.49	-0.36	-10.339	-0.366	3/2-	11/2-
173	94	1344.69	1346.47	1347.365	20.64	1.17	11.15	-0.16	-10.256	-0.616		11/2-
174	95	1353.79	1355.59	1356.678	20.25	1.22	9.10	-0.33	-10.150	-0.842	5/2-	11/2-
175	96	1364.77	1367.18	1368.079	20.07	1.63	10.97	-0.15	-10.116	-2.087		1/2+
176	97	1374.57	1376.26	1377.268	20.78	1.99	9.81	-0.05	-10.269	-0.588	5/2+	3/2-
177	98	1385.31	1387.42	1388.364	20.54	2.45	10.74	0.19	-10.160	-0.793		3/2-

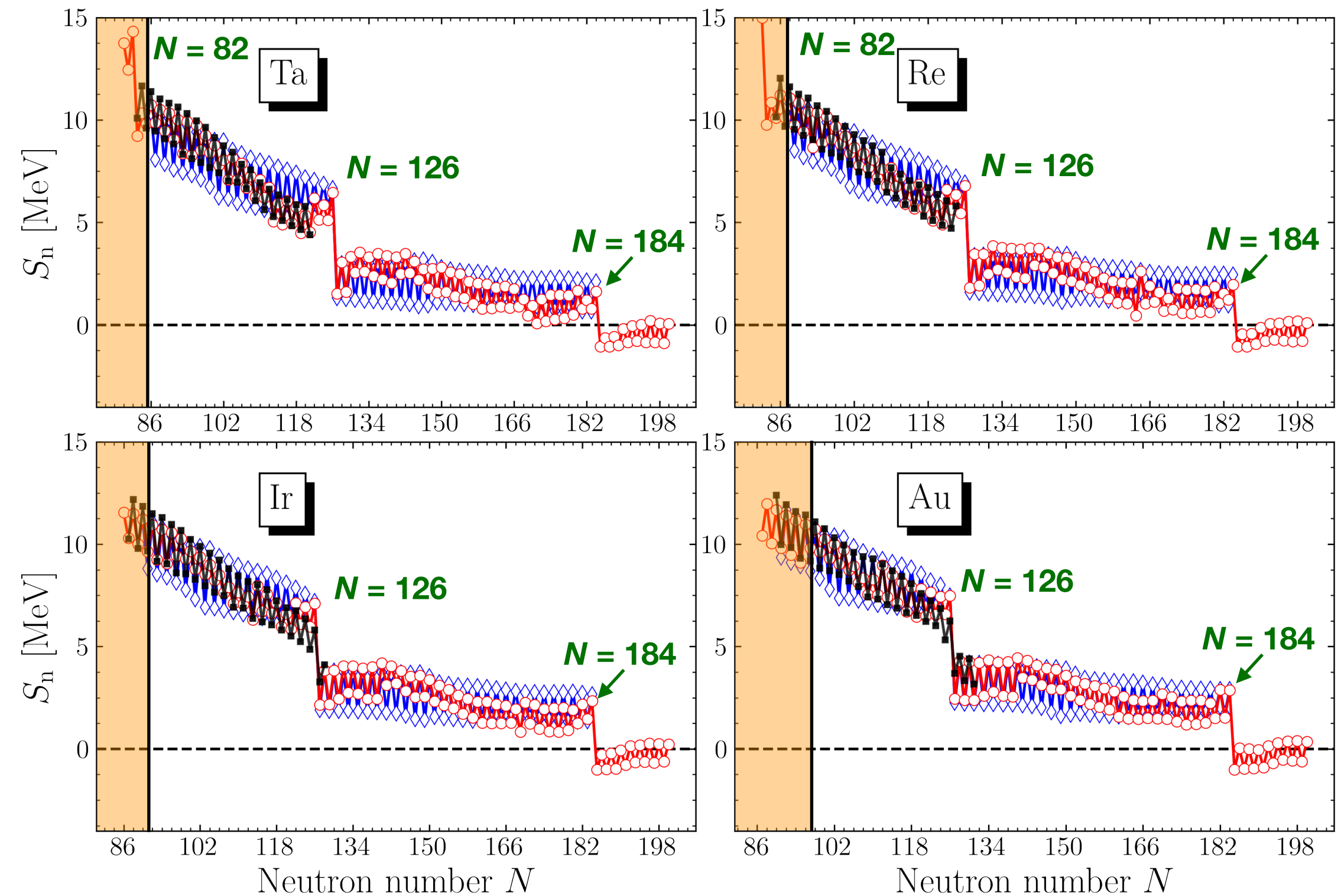
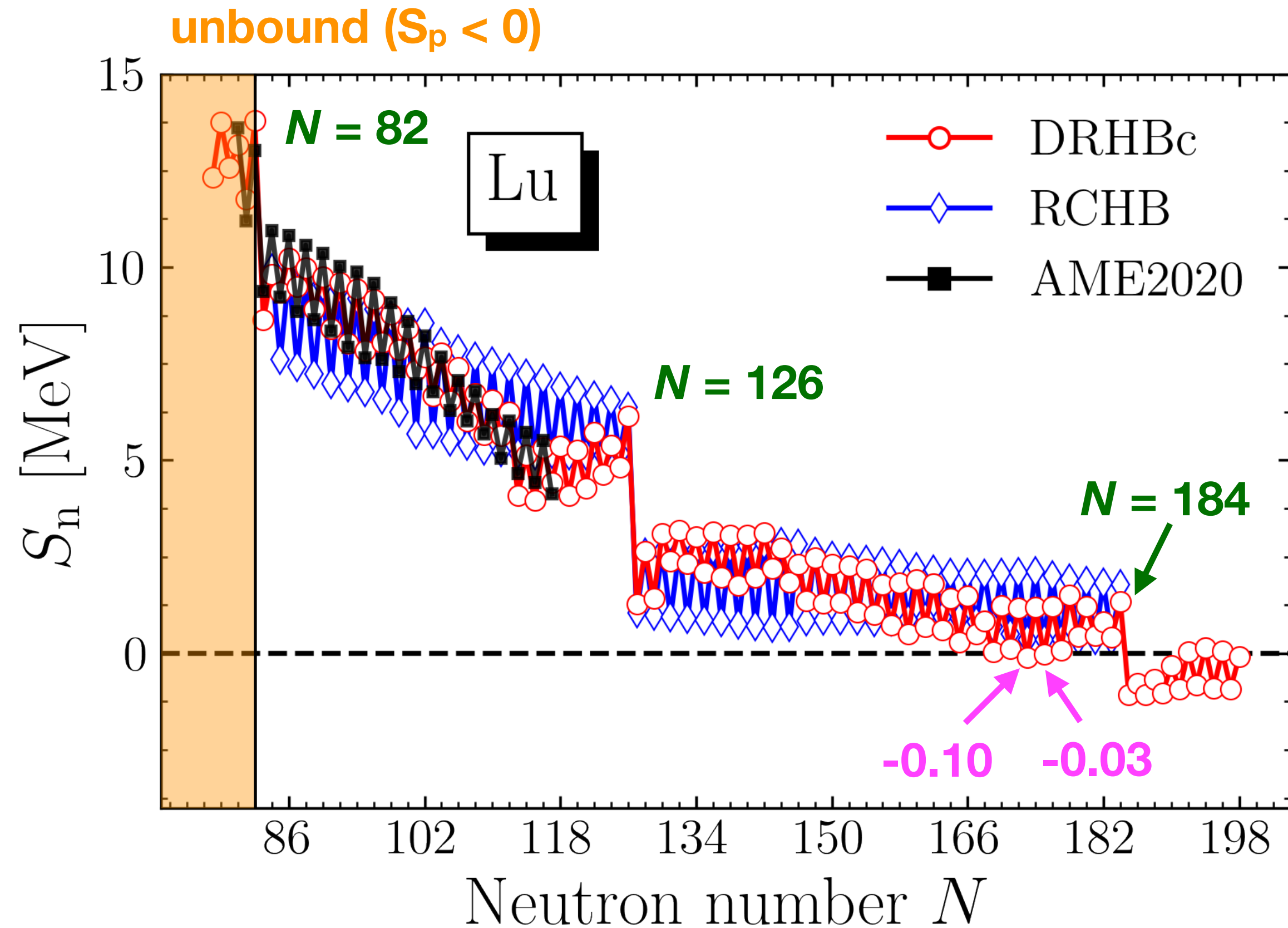
- The proton drip line for  $71 \leq Z \leq 79$  odd- $Z$  nuclei is determined by the one-proton separation energies.

# Comparisons of odd- $Z$ nuclei



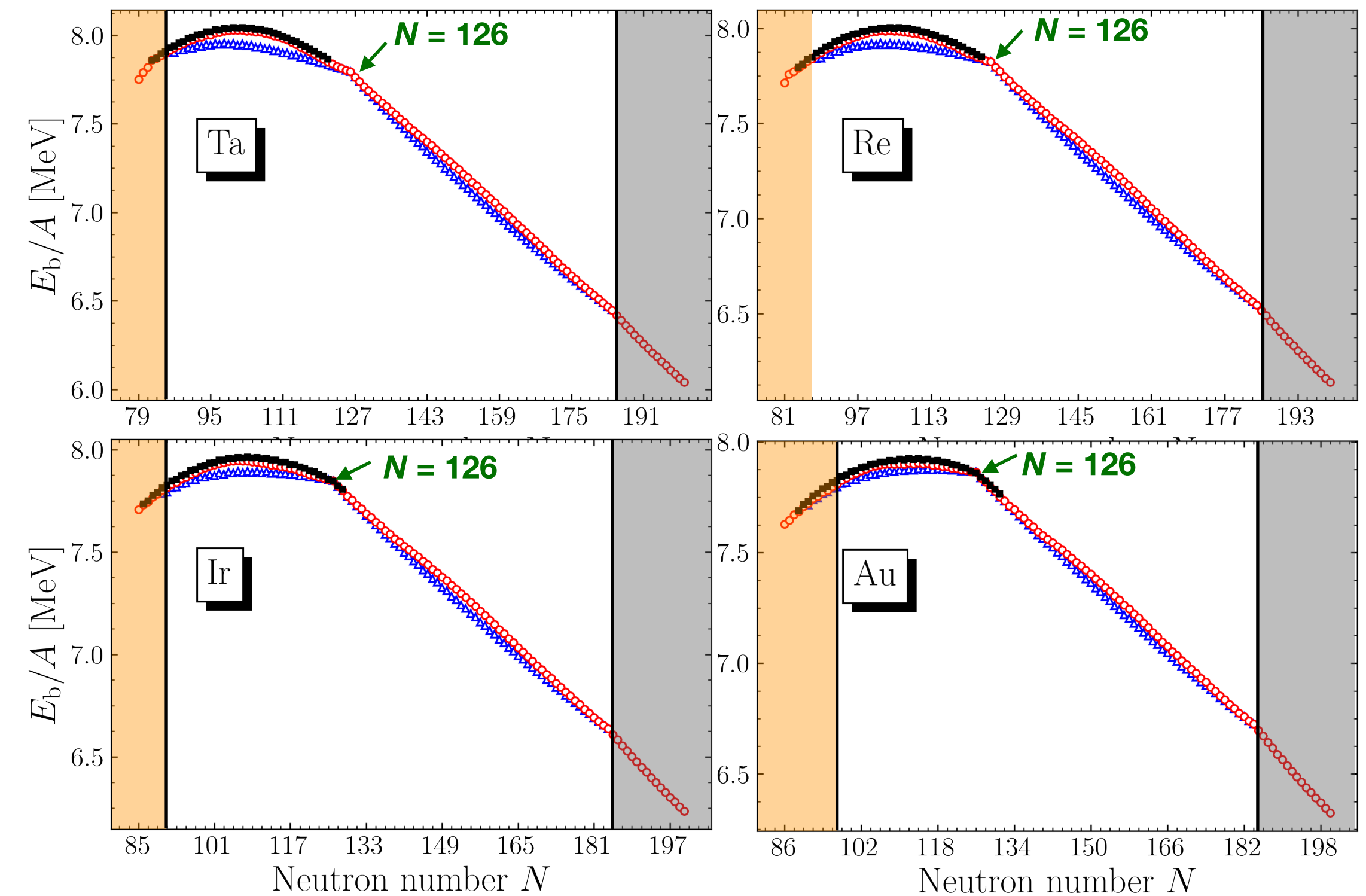
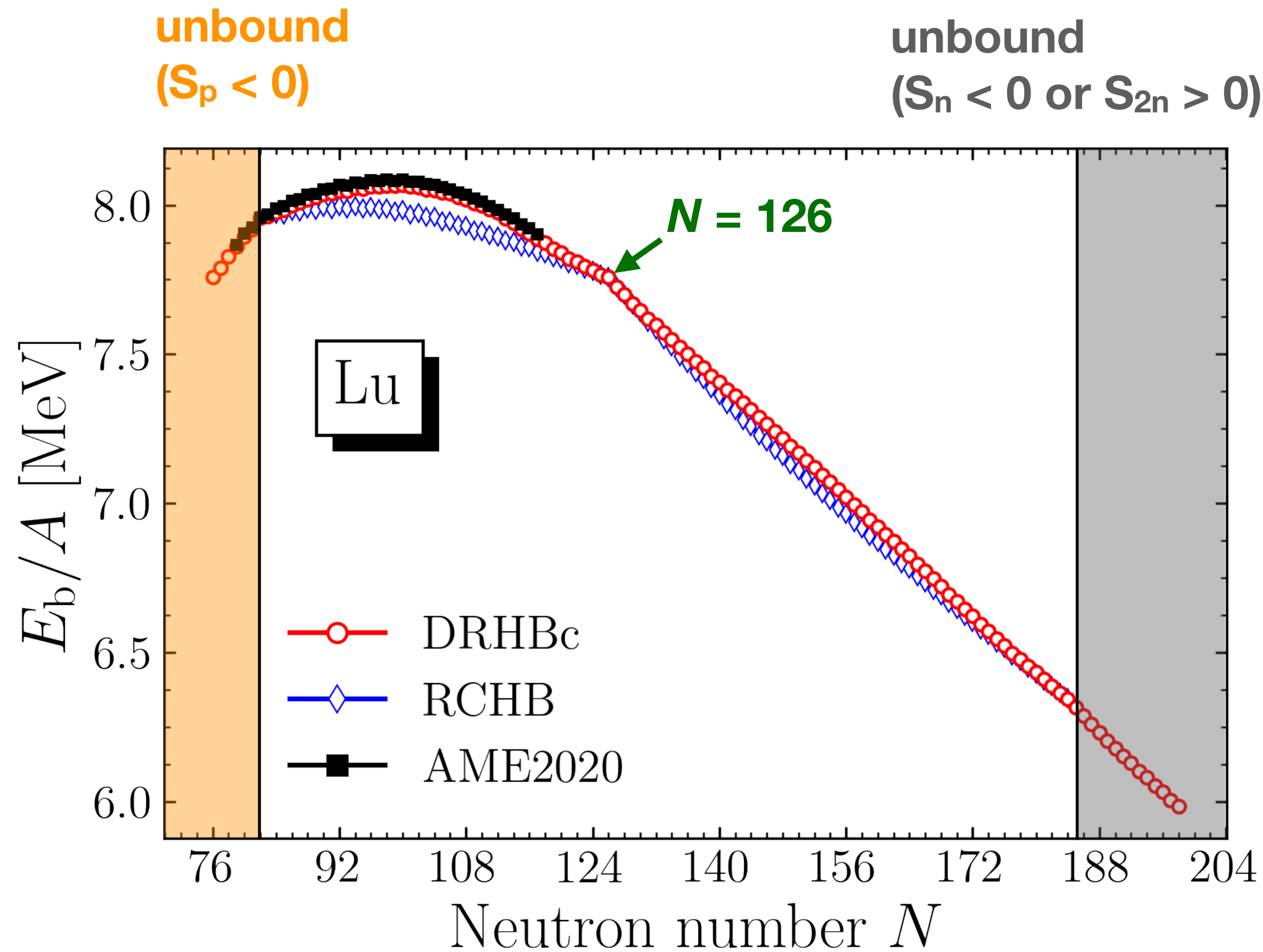
- Two-neutron separation energies with DRHBc theory well predict experimental data.

# Comparisons of odd- $Z$ nuclei



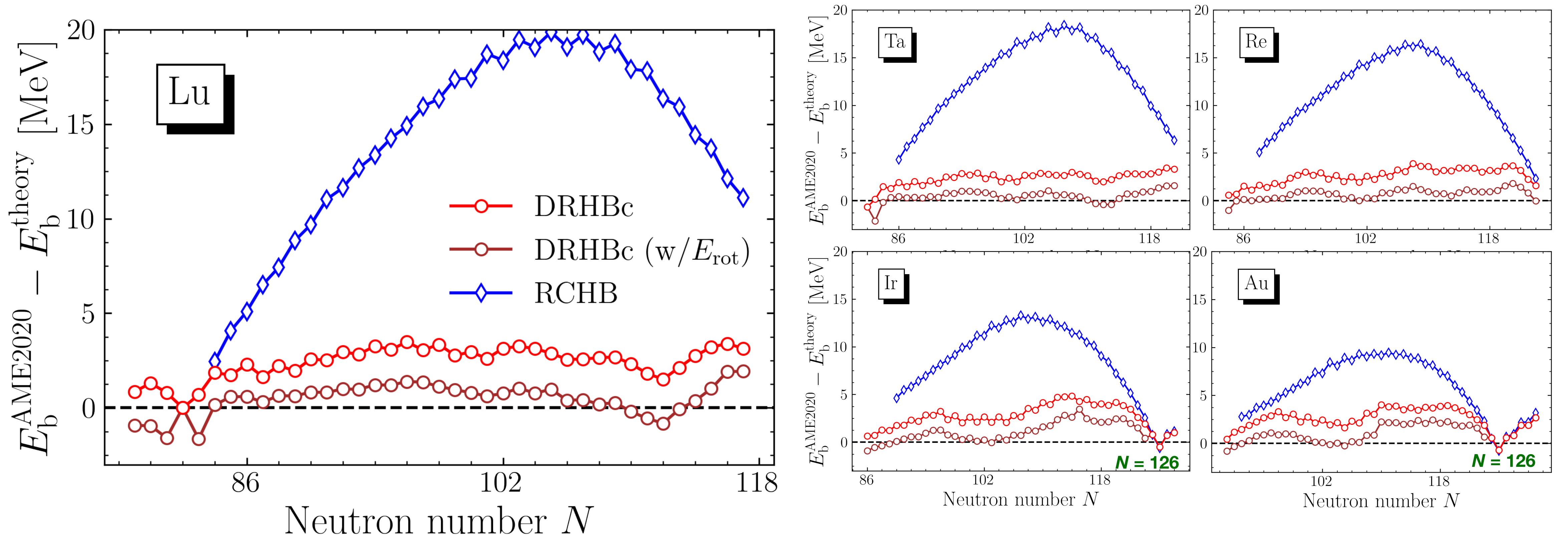
- The patterns of one-neutron separation energies are well reproduced in DRHBc theory.
- The one-neutron separation energies of  $^{244}\text{Lu}$  and  $^{246}\text{Lu}$  are less than 0.
- The nuclei with  $N > 184$  are unbound (even- $Z$  nuclei also).

# Comparisons of odd- $Z$ nuclei



- The binding energies described by DRHBc show less discrepancy with the experimental data than those by RCHB.

# Comparisons of odd- $Z$ nuclei

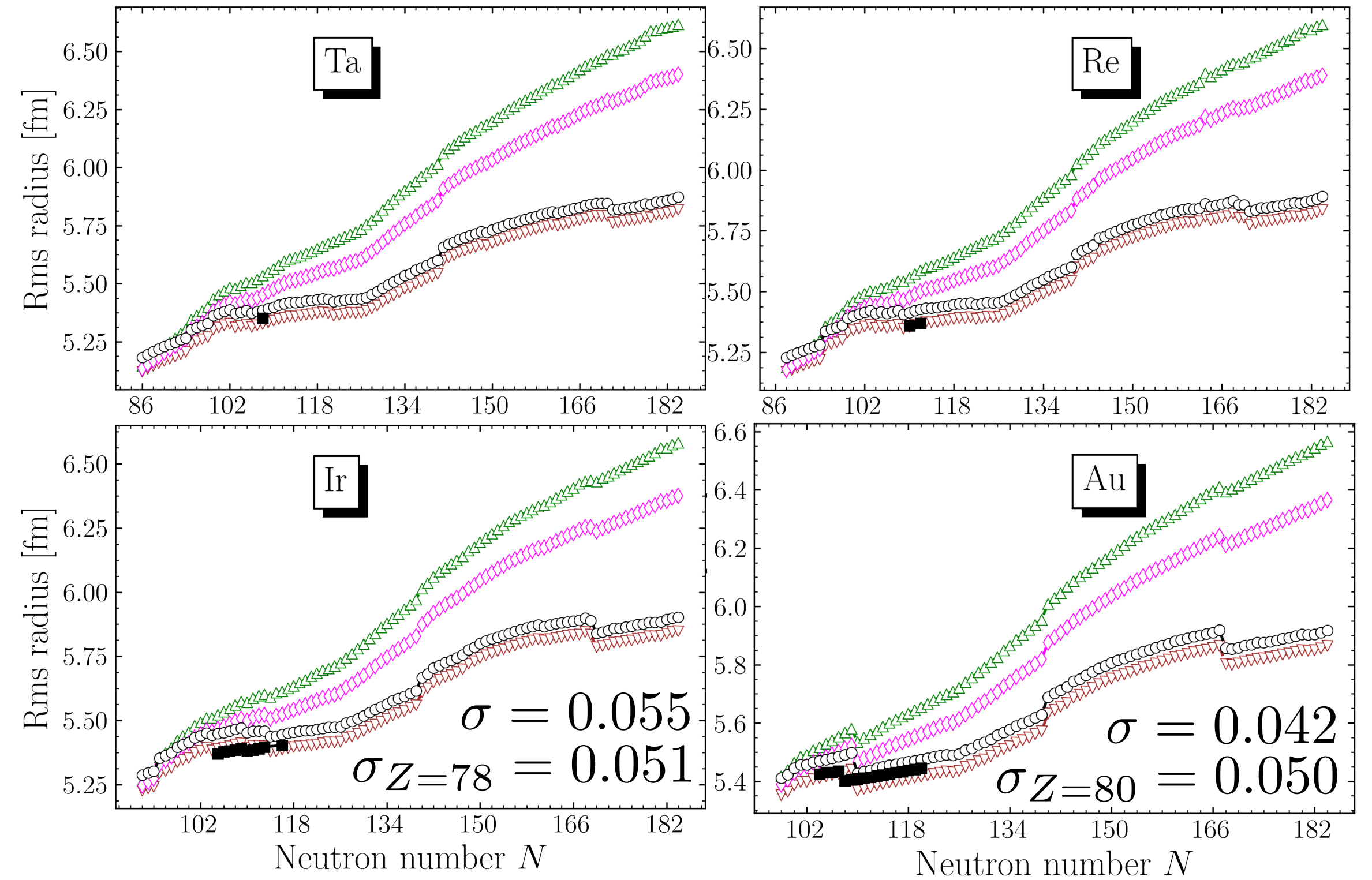
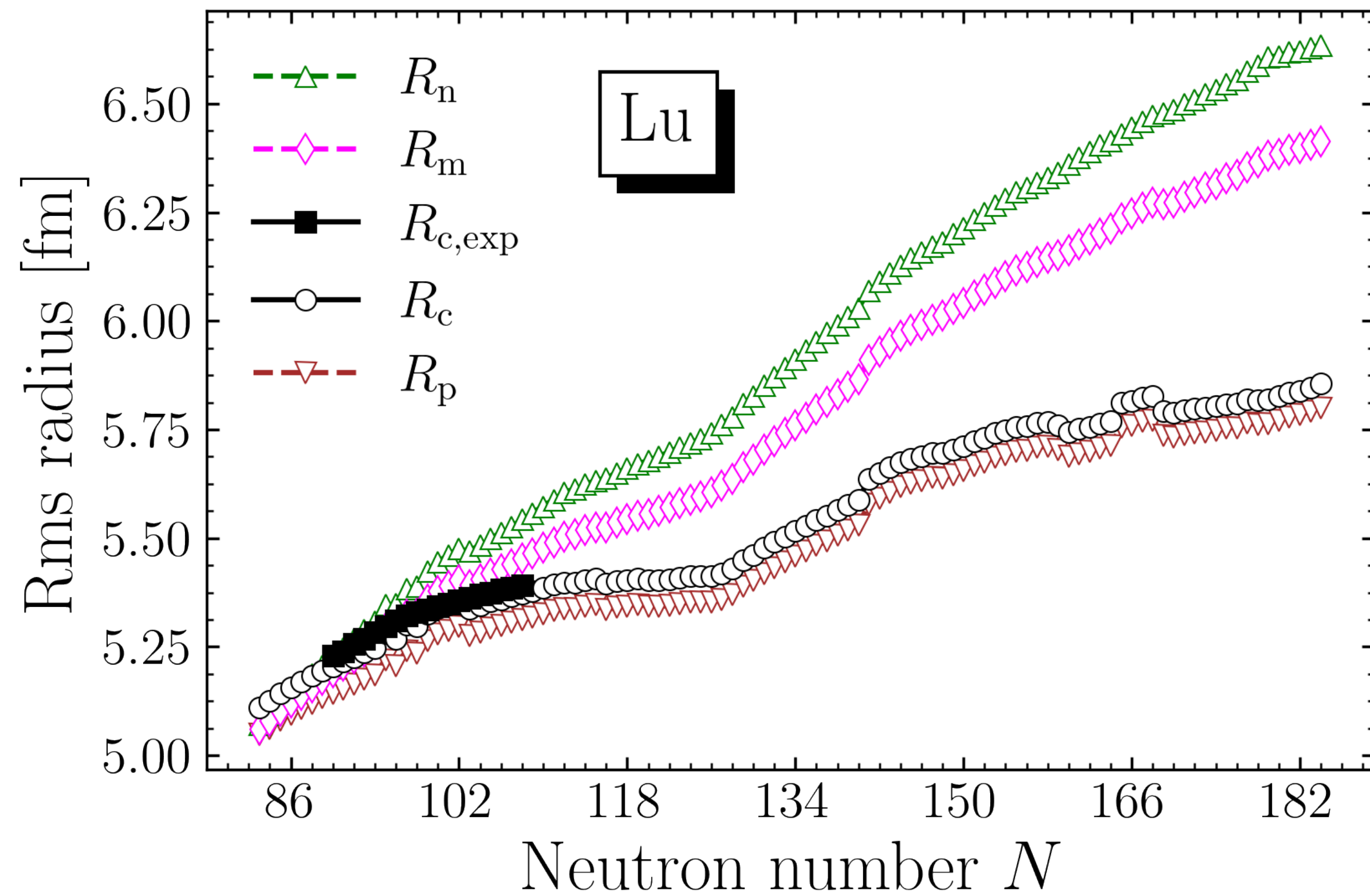


rms deviation

$\sigma$ [MeV]	Lu	Hf	Ta	W	Re	Os	Ir	Pt	Au	Pt
$E_b$	2.55	2.90	2.44	3.00	2.72	3.51	2.98	3.53	2.74	2.96
$E_{b+\text{rot}}$	0.95	0.85	0.790	0.89	0.87	1.47	1.45	1.71	1.42	1.22

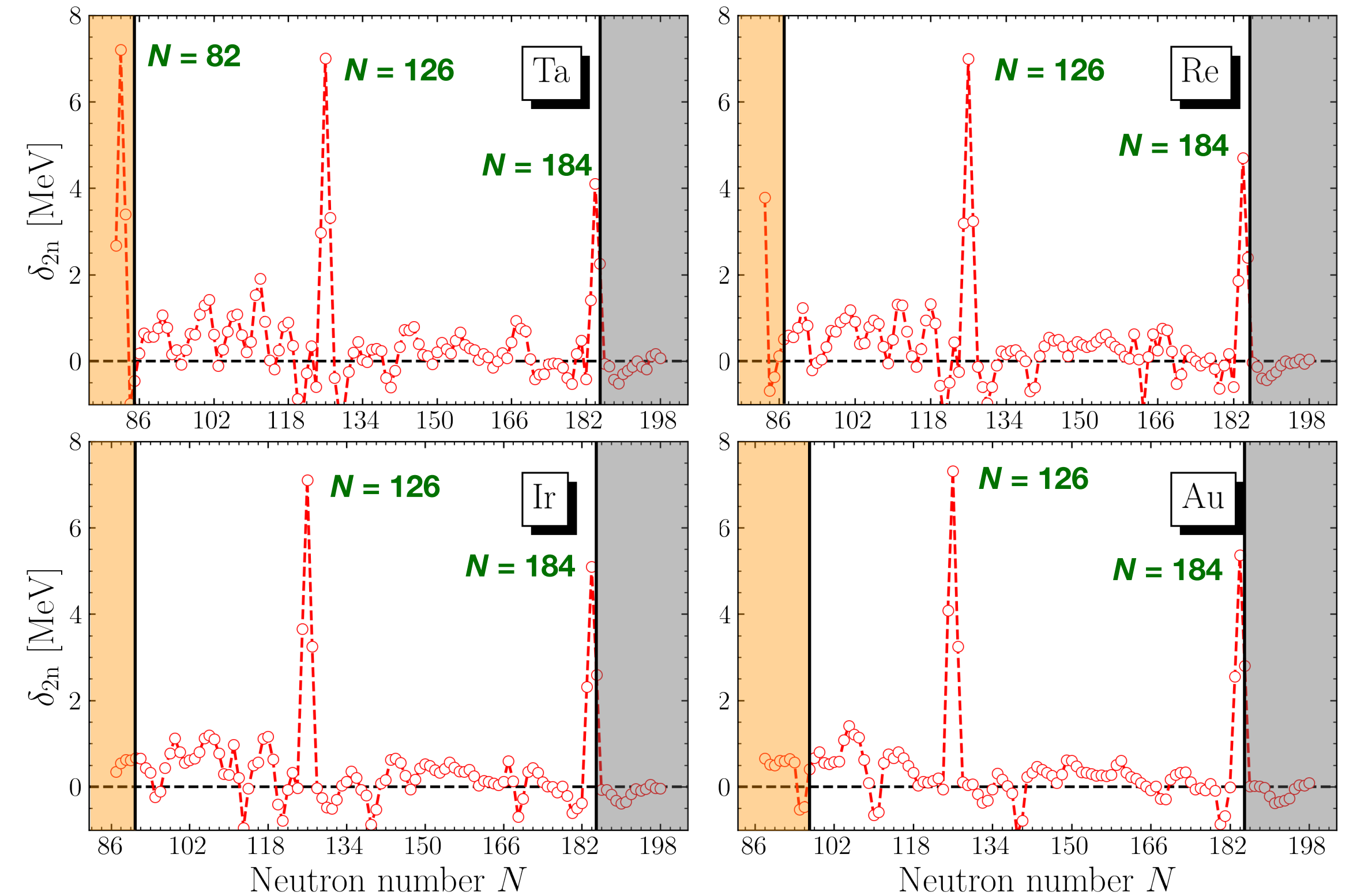
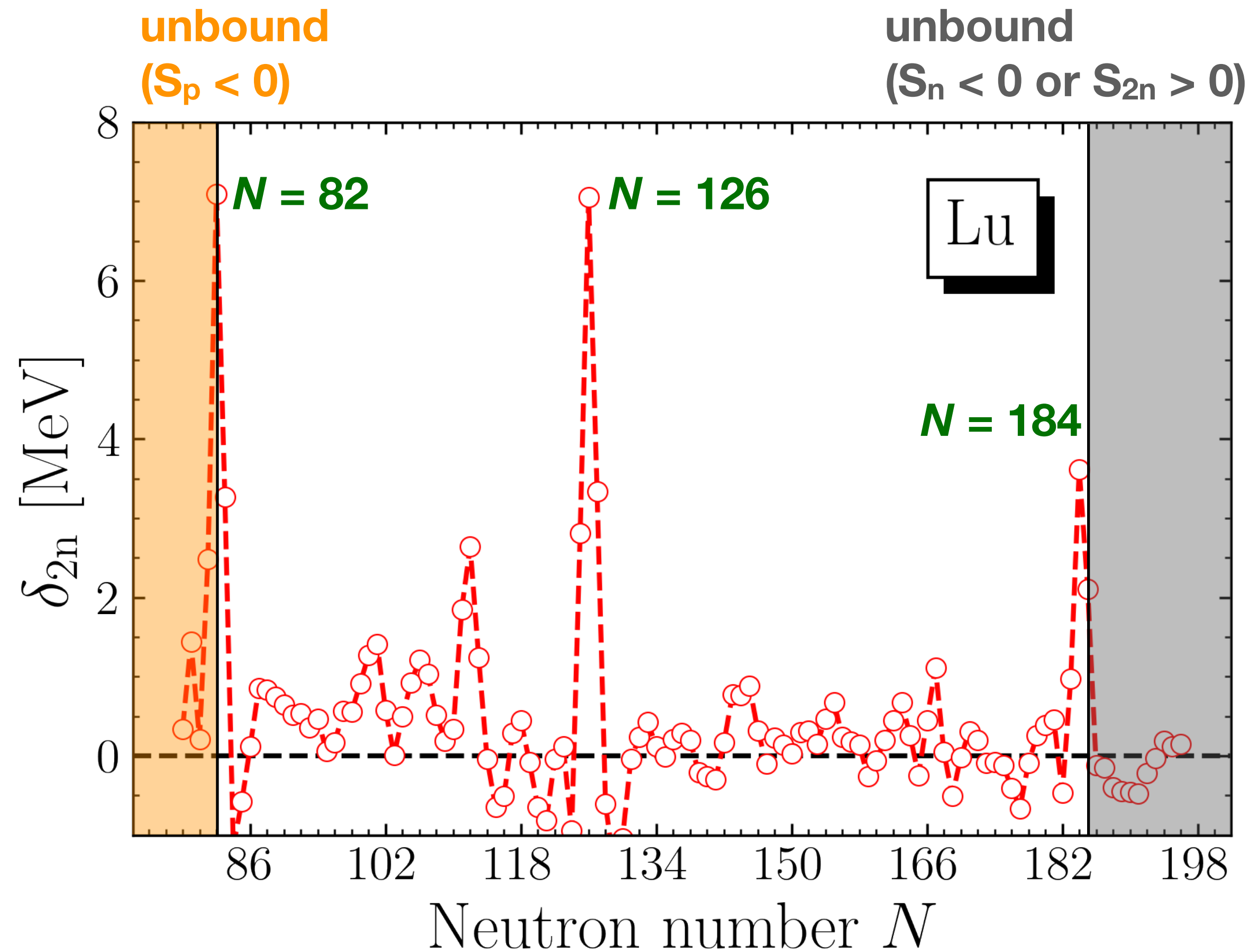


# Properties of odd- $Z$ nuclei



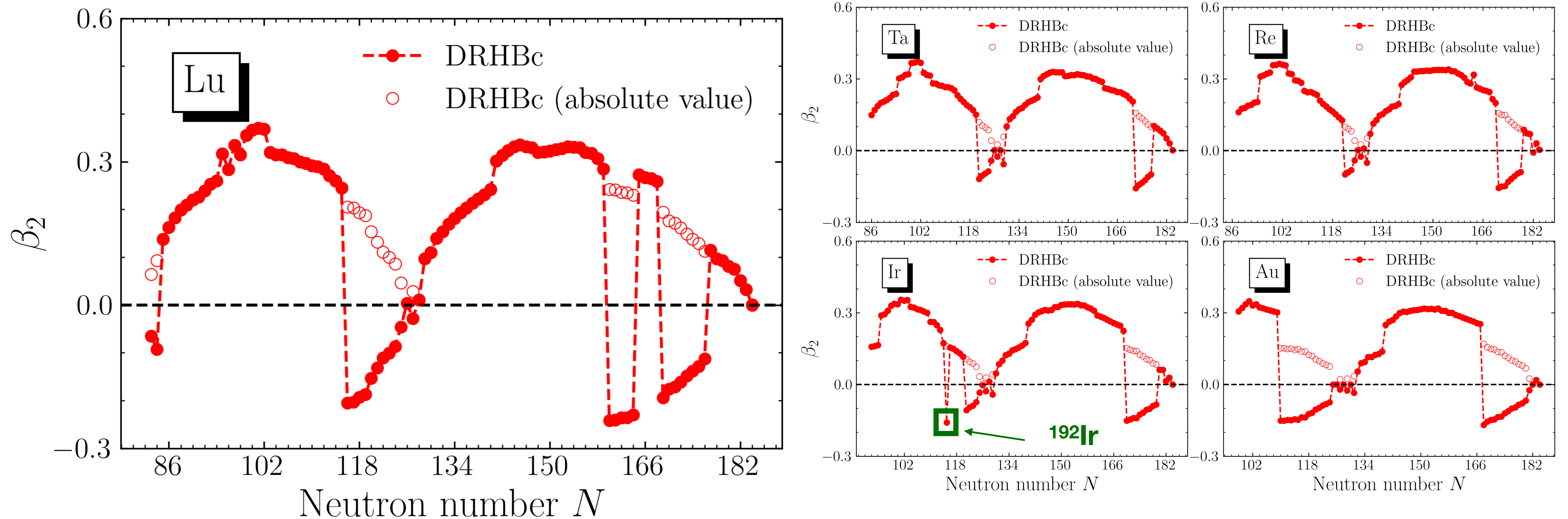
- For Lu isotopes, predicted  $R_c$  values are larger than experimental data.
- However, For Ir and Au isotopes, predicted  $R_c$  values are smaller than experimental data.

# Properties of odd- $Z$ nuclei



- The nuclei with neutron magic number are also stable in odd- $Z$  nuclei.

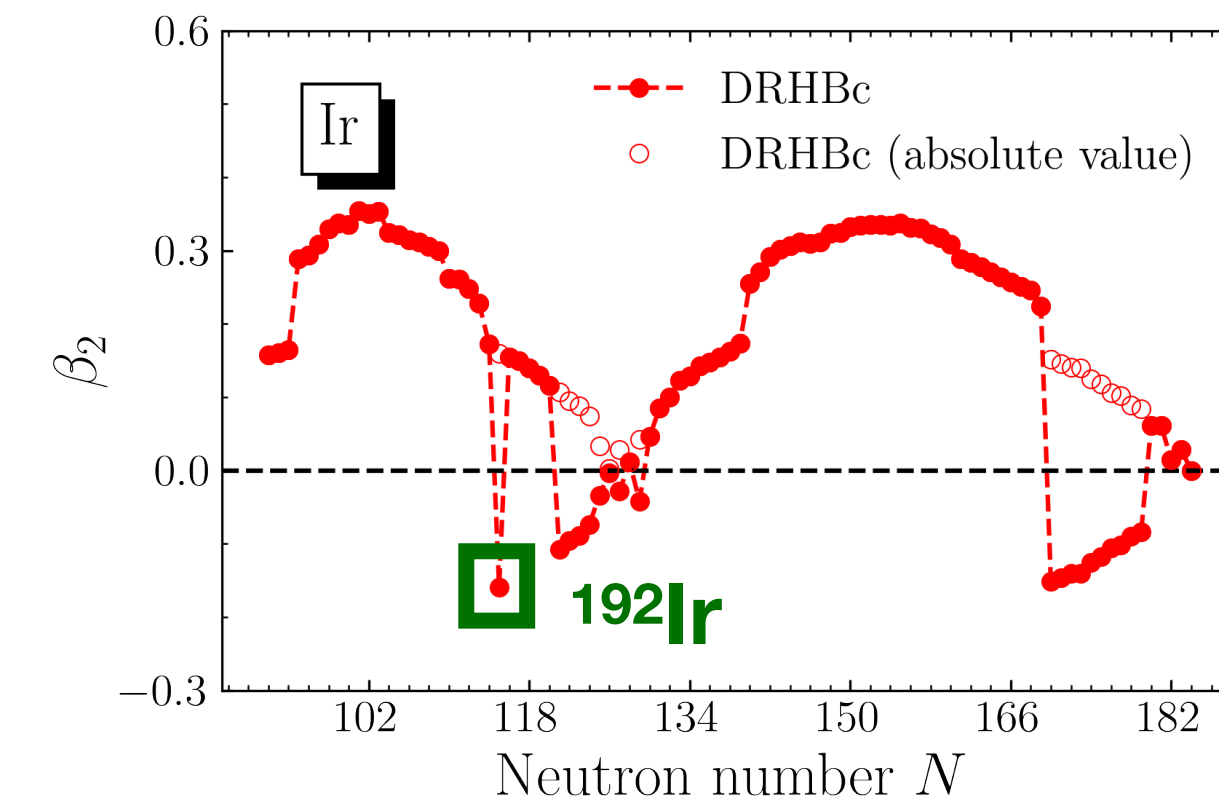
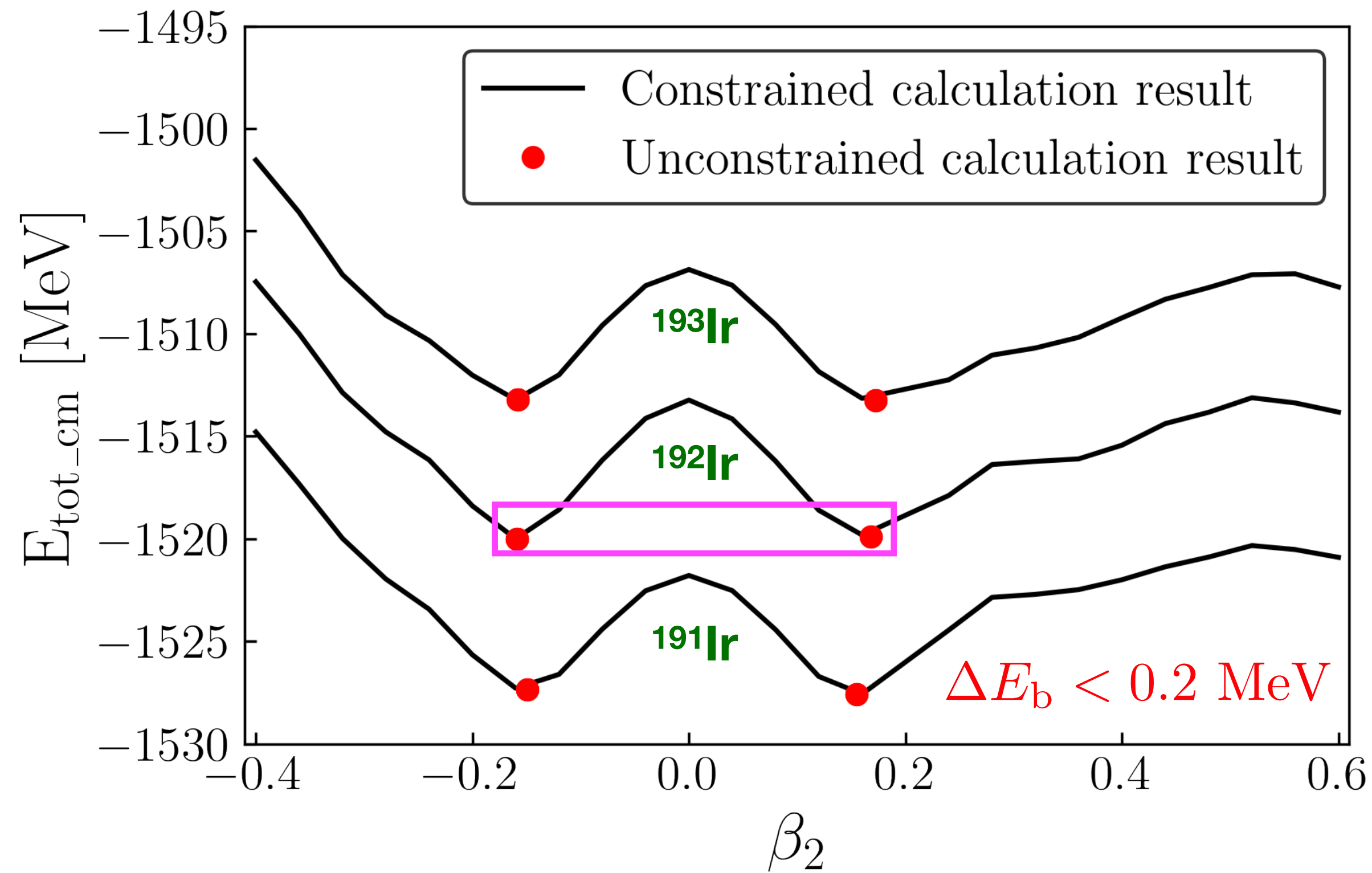
# Properties of odd- $Z$ nuclei



- Abrupt Changes of nuclear shapes are related to shape coexistence.

# Properties of odd- $Z$ nuclei

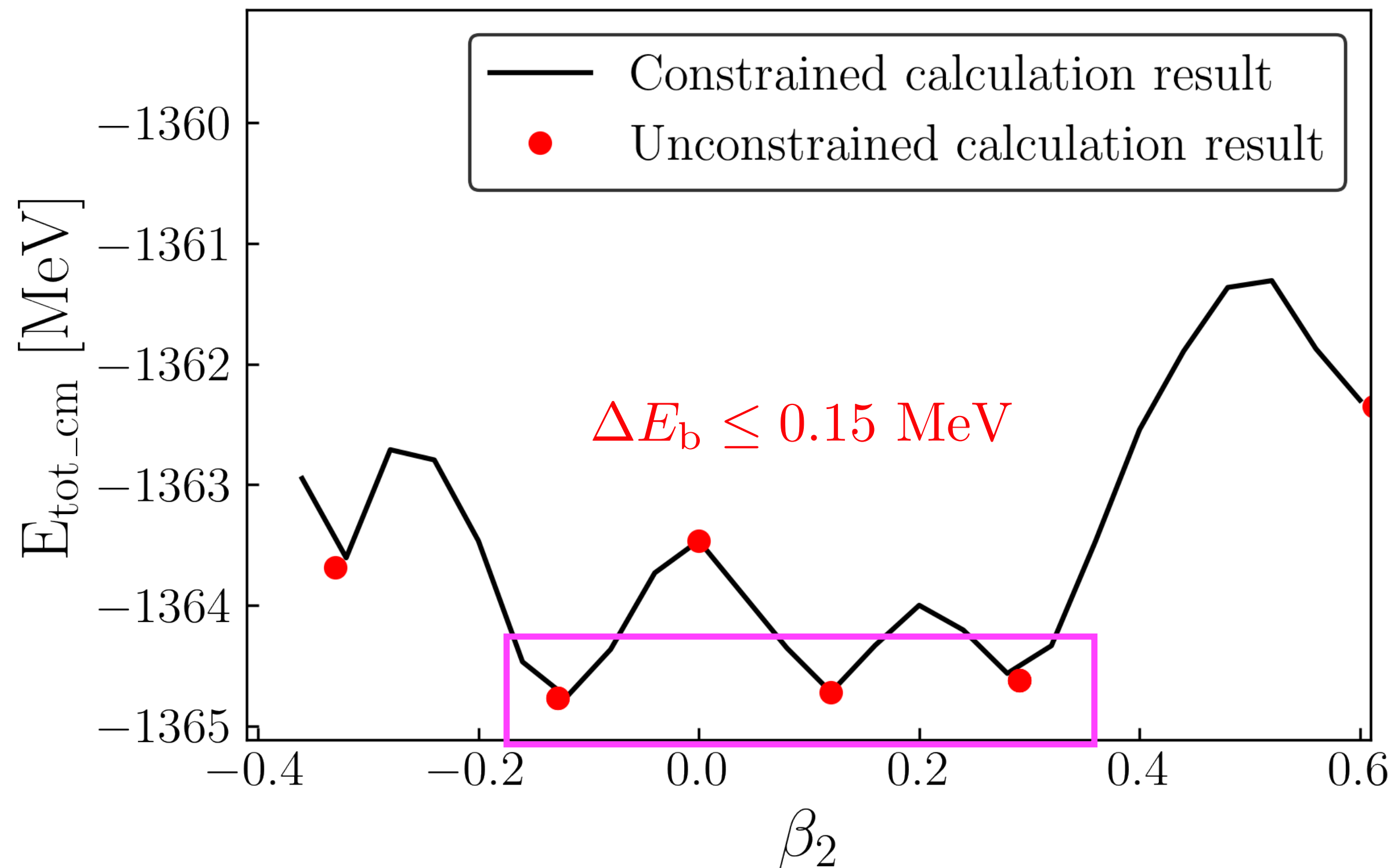
## Potential energy curves



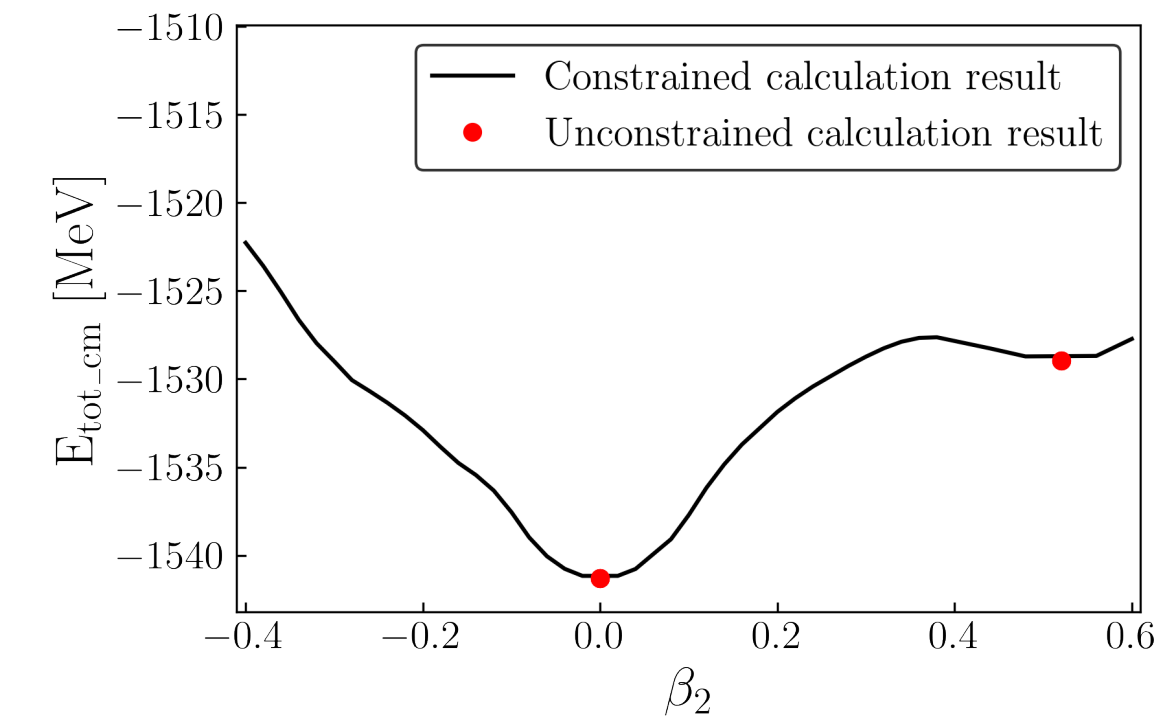
- The  $^{192}\text{Ir}$  isotope exhibits the shape coexistence with  $\Delta E_b < 0.2$  MeV.

# Properties of odd- $Z$ nuclei

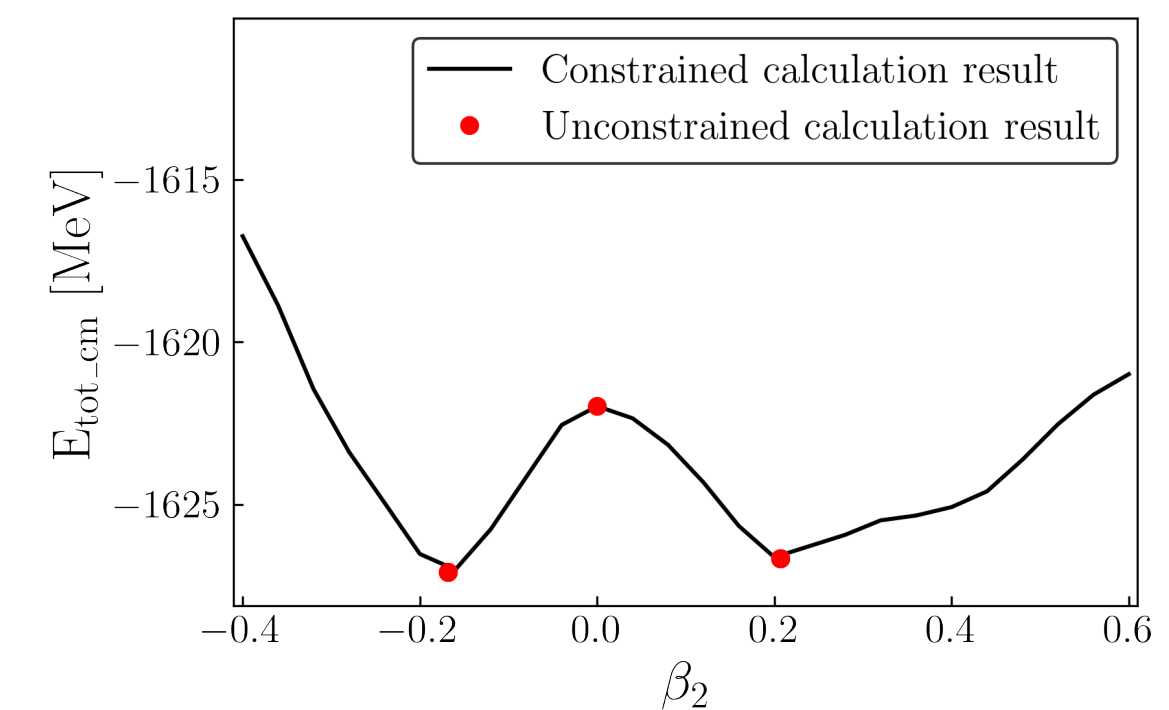
Au-175 (converged points)



Hf-198 (converged points)

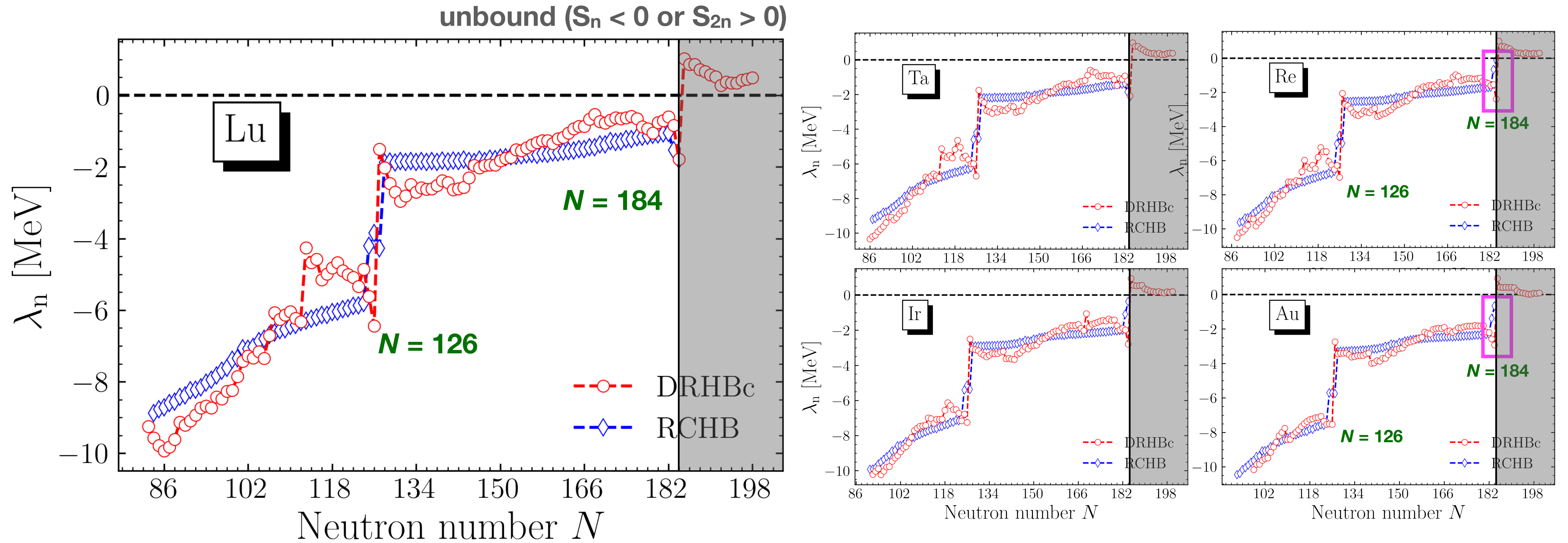


Hf-243 (converged points)



- There is new type of PEC in Au isotopes.

# Properties of odd- $Z$ nuclei



- At the magic number, neutron Fermi surface is low.
- The results from DRHBc show consistent in neutron drip line.

# Summary

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- The ground states of  $71 \leq Z \leq 79$  odd- $Z$  (about 500) bound nuclei have been determined.
- Some of the calculation results of odd- $Z$  nuclei were compared with experimental data and RCHB.
- The results from DRHBc describe the experimental data qualitatively well.

Thank you for your attention!